# **Electronically coarse grained water**

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# Challenge:extending the transferability of empirical potentialsOur solution:coarse grained electronic structure

A. Jones, **Quantum drude oscillators for accurate many-body intermolecular forces**, PhD thesis, The University of Edinburgh

A. Jones, F. Cipcigan, V. Sokhan, J. Crain, G. Martyna, **Electronically coarse grained model for** water, PRL 110, 227801 (2013)



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# 1. Quantum Drude Oscillator (QDO)

Light **negative** particle tethered harmonically to heavy **positive**, oppositely charged nucleus

#### Free parameters

 $\mu$ : reduced mass  $\omega$ : spring constant q: charge

#### Response

Polarisation: 
$$\alpha_l = \left[\frac{q^2}{\mu\omega^2}\right] \left[\frac{(2l-1)!!}{l}\right] \left[\frac{\hbar}{2\mu\omega}\right]^{l-1}$$

Dispersion: 
$$C_6 = \frac{3}{4} \alpha_1 \alpha_1 \hbar \omega$$
,  
 $C_8 = 5 \alpha_1 \alpha_2 \hbar \omega$ ,  
 $C_{10} = \left[\frac{21}{2} \alpha_1 \alpha_3 + \frac{70}{4} \alpha_2 \alpha_2\right] \hbar \omega$ 

#### 2. Invariants predicted by QDOs

Polarisation: 
$$\sqrt{\frac{20}{9}} \frac{\alpha_2}{\sqrt{\alpha_1 \alpha_3}} = 1$$
 Dispersion:  $\sqrt{\frac{49}{40}} \frac{C_8}{\sqrt{C_6 C_{10}}} = 1$ 



![](_page_2_Figure_3.jpeg)

![](_page_2_Figure_4.jpeg)

## 3. QDO-water model

Frame: ground state moments

![](_page_3_Figure_2.jpeg)

**QDO:** molecular response

![](_page_3_Figure_4.jpeg)

 $\mu$  = 0.3656 amu  $\omega$  = 0.6287  $\omega_h$ q = -1.1973 e

4. QDO-water model (continued)

Short range interactions

![](_page_4_Figure_2.jpeg)

# 5. Efficient sampling: APIMD-QDO

(Adiabatic Path Integral Molecular Dynamics applied to QDOs)

1. Write partition function of N particles as path integral, P slices  

$$Z(\beta) = \operatorname{tr} \hat{\rho}(\beta) = \int \mathbf{d}^P \vec{x} \prod_{i=1}^P \rho(\vec{x}_i, \vec{x}_{i+1}; \tau) \quad \tau = \beta/P$$

2. Define effective (classical) potential of N×P particles

$$Z(\beta) = \int \mathbf{d}^P \vec{x} \exp\left[-\beta \phi_{\text{eff}}\left(\vec{x}_1, \vec{x}_2, \dots, \vec{x}_P\right)\right]$$
$$\phi_{\text{eff}}\left(\vec{x}_1, \vec{x}_2, \dots, \vec{x}_P\right) = -\frac{1}{\beta} \sum_{i=1}^P \log\left[\rho\left(\vec{x}_i, \vec{x}_{i+1}; \tau\right)\right]$$

3. Approximate resulting high temperature density matrices  $\rho(\vec{x}, \vec{x}'; \tau) \equiv \langle \vec{x} | e^{-\tau (\hat{H}_0 + \hat{V})} | \vec{x}' \rangle$   $= \langle \vec{x} | e^{-\frac{\tau}{2} \hat{V}} e^{-\tau \hat{H}_0} e^{-\frac{\tau}{2} \hat{V}} | \vec{x}' \rangle + \mathcal{O}(\tau^3)$ 

### 6. Liquid QDO-water

#### **Radial distribution function**

![](_page_6_Figure_2.jpeg)

Vapour pressure 46 ± 2 kJ / mol exp: 43.91 kJ/mol

# Dielectric constant $79 \pm 2$

exp: 78

Surface tension 72.6 ± 1 mN / m exp: 71.73 mN / m 7. Liquid-vapour interface (unoptimised model)

Density and dipole moment

![](_page_7_Figure_2.jpeg)

**Electronic distribution** (ground state distribution substracted)

1Å 13 Å 15 Å

charge loss charge gain

Surface charge density

![](_page_8_Figure_2.jpeg)

Surface expansion of nearest neighbour distance by 1–2% (only classical model with a surface expansion)

![](_page_9_Figure_2.jpeg)

Weaker hydrogen bond at the surface

![](_page_10_Figure_2.jpeg)

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The hydrogen bond forms in the valleys of the PMF (Potential of Mean Force)

How are hydrogen bonds broken?

![](_page_11_Picture_2.jpeg)

#### Tetrahedrality

#### Number of hydrogen bonds

![](_page_12_Figure_3.jpeg)